

Lösung A1

- a) $\sqrt[3]{3^6} = 3^2 = 9$
- b) $\sqrt[4]{4^8} = 4^2 = 16$
- c) $\sqrt[5]{2^{15}} = 2^3 = 8$
- d) $\sqrt[3]{3^9} = 3^3 = 27$
- e) $\sqrt{4^6} = 4^3 = 64$
- f) $(\sqrt[5]{a})^4 = \sqrt[5]{a^4}$
- g) $(\sqrt[4]{b})^4 = \sqrt[4]{b^4} = b$
- h) $(\sqrt[3]{x})^5 = \sqrt[3]{x^5} = x\sqrt[3]{x^2}$
- i) $(\sqrt[3]{y^2})^3 = y^2$
- j) $(\sqrt[5]{z^2})^3 = \sqrt[5]{z^6} = z\sqrt[5]{z}$

Lösung A2

- a) $\sqrt[3]{a^6b^9} = a^2b^3$
- b) $\sqrt[4]{x^{12}y^8} = x^3y^2$
- c) $\sqrt[6]{a^3} = \sqrt{a}$
- d) $\sqrt[6]{b^2} = \sqrt[3]{b}$
- e) $\sqrt[8]{x^2y^4} = \sqrt[4]{xy^2}$
- f) $\sqrt{\sqrt{81}} = \sqrt[4]{81} = 3$
- g) $\sqrt{\sqrt[3]{64}} = \sqrt[6]{64} = 2$
- h) $\sqrt[3]{\sqrt{64}} = \sqrt[6]{64} = 2$
- i) $\sqrt[3]{\sqrt[3]{512}} = \sqrt[9]{512} = 2$
- j) $\sqrt{\sqrt{16}} = \sqrt[4]{16} = 2$

Lösung A3

- a) $\sqrt{\sqrt{a^4}} = \sqrt[4]{a^4} = a$
- b) $\sqrt{\sqrt[3]{b^6}} = \sqrt[6]{b^6} = b$
- c) $\sqrt[3]{\sqrt[3]{c^9}} = \sqrt[9]{c^9} = c$
- d) $\sqrt{\sqrt{x^8}} = \sqrt[4]{x^8} = x^2$
- e) $\sqrt[3]{\sqrt{y^{12}}} = \sqrt[6]{y^{12}} = y^2$

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- f) $\sqrt[3]{\sqrt[3]{a^4}} = \sqrt[6]{a^4} = \sqrt[3]{a^2}$
- g) $\sqrt[3]{\sqrt[3]{b^6}} = \sqrt[9]{b^6} = \sqrt[3]{b^2}$
- h) $\sqrt[3]{\sqrt[4]{c^{10}}} = \sqrt[12]{c^{10}} = \sqrt[6]{c^5}$
- i) $\sqrt[3]{x^{12}} = \sqrt[6]{x^{12}} = x^2$
- j) $\sqrt{\sqrt{y^6}} = \sqrt[4]{y^6} = y \cdot \sqrt[4]{y^2} = y \cdot \sqrt{y}$

Lösung A4

- a) $\frac{\sqrt{a}}{a^{\frac{1}{4}}} = a^{\frac{1}{4}} = \sqrt[4]{a}$
- b) $\frac{\sqrt[3]{x^2}}{x^{\frac{1}{6}}} = x^{\frac{3}{6}} = x^{\frac{1}{2}} = \sqrt{x}$
- c) $\frac{5^{\frac{1}{n-1}}}{5^{\frac{1}{n-1}}} = 1$
- d) $\left(\left(\frac{1}{4}\right)^{-a}\right)^{\frac{1}{a}} = \left(\frac{1}{4}\right)^{-1} = 4$
- e) $\sqrt{\frac{4x^2}{5y^2}} = \frac{2x}{y\sqrt{5}} = \frac{2x\sqrt{5}}{y\cdot\sqrt{5}\cdot\sqrt{5}} = \frac{2x\sqrt{5}}{5y}$
- f) $\sqrt[3]{\frac{x}{b^2}} \cdot \sqrt[3]{\frac{x^2}{b}} = \frac{x}{b}$
- g) $\sqrt{x^3y^2} \cdot \frac{1}{\sqrt{xy}} = x \cdot \sqrt{y}$
- h) $\frac{\sqrt[3]{x}}{\sqrt[3]{xy^2}} = \frac{1}{\sqrt[3]{y^3}} = \frac{1}{y}$